<u>CSA Mock Exam 1</u>: administered on AP Live 05/04/2020 Question 2: Methods & Control Structures plus open-ended question

Directions: SHOW ALL YOUR WORK. REMEMBER THAT PROGRAM SEGMENTS ARE TO BE WRITTEN IN JAVA.

Notes:

- Assume that the classes listed in the Java Quick Reference have been imported where appropriate.
- Unless otherwise noted in the question, assume that parameters in method calls are not null and that methods are called only when their preconditions are satisfied.
- In writing solutions for each question, you may use any of the accessible methods that are listed in classes defined in that question. Writing significant amounts of code that can be replaced by a call to one of these methods will not receive full credit.

2.

A mathematical sequence is an ordered list of numbers. This question involves a sequence called a *hailstone* sequence. If n is the value of a term in the sequence, then the following rules are used to find the next term, if one exists.

- If *n* is 1, the sequence terminates.
- If *n* is even, then the next term is $\frac{n}{2}$.
- If *n* is odd, then the next term is 3n + 1.

For this question, assume that when the rules are applied, the sequence will eventually terminate with the term n = 1.

The following are examples of hailstone sequences.

Example 1: 5, 16, 8, 4, 2, 1

- The first term is 5, so the second term is 5 * 3 + 1 = 16.
- The second term is 16, so the third term is $\frac{16}{2} = 8$.
- The third term is 8, so the fourth term is $\frac{8}{2} = 4$.
- The fourth term is 4, so the fifth term is $\frac{4}{2} = 2$.
- The fifth term is 2, so the sixth term is $\frac{2}{2} = 1$.
- Since the sixth term is 1, the sequence terminates.

Example 2: 8, 4, 2, 1

- The first term is 8, so the second term is $\frac{8}{2} = 4$.
- The second term is 4, so the third term is $\frac{4}{2} = 2$.
- The third term is 2, so the fourth term is $\frac{2}{2} = 1$.
- · Since the fourth term is 1, the sequence terminates.

The Hailstone class, shown below, is used to represent a hailstone sequence. You will write one method and respond to one open-ended question about the Hailstone class.

```
public class Hailstone
{
    /** Returns the length of a hailstone sequence that starts with n,
    * as described in part (a).
     * Precondition: n > 0
     */
   public static int hailstoneLength(int n)
    { /* to be implemented in part (a) */ }
    /** Returns true if the hailstone sequence that starts with n is considered long
     * and false otherwise, as described in part (b).
     * Precondition: n > 0
     */
   public static boolean isLongSeg(int n)
    { /* to be implemented in part (b) */ }
    /** Returns the proportion of the first n hailstone sequences that are considered long,
     * as described in part (c).
     * Precondition: n > 0
     */
   public static double propLong(int n)
    { /* to be implemented in part (c) */ }
```

// There may be instance variables, constructors, and methods not shown.

}

(a) The length of a hailstone sequence is the number of terms it contains. For example, the hailstone sequence in example 1 (5, 16, 8, 4, 2, 1) has a length of 6 and the hailstone sequence in example 2 (8, 4, 2, 1) has a length of 4.

Write the method hailstoneLength(int n), which returns the length of the hailstone sequence that starts with n.

/** Returns the length of a hailstone sequence that starts with n, as described in part (a).

```
* Precondition: n > 0
*/
public static int hailstoneLength(int n)
```

A hailstone sequence is considered long if its length is greater than its starting value. For example, the hailstone sequence in example 1 (5, 16, 8, 4, 2, 1) is considered long because its length (6) is greater than its starting value (5). The hailstone sequence in example 2 (8, 4, 2, 1) is not considered long because its length (4) is less than or equal to its starting value (8).

The method propLong(int n) returns the proportion of long hailstone sequences with starting values between 1 and n, inclusive.

Consider the following table, which provides data about the hailstone sequences with starting values between 1 and 10, inclusive.

Starting Value	Terms in the Sequence	Length of the Sequence	Long?
1	1	1	No
2	2, 1	2	No
3	3, 10, 5, 16, 8, 4, 2, 1	8	Yes
4	4, 2, 1	3	No
5	5, 16, 8, 4, 2, 1	6	Yes
6	6, 3, 10, 5, 16, 8, 4, 2, 1	9	Yes
7	7, 22, 11, 34, 17, 52, 26, 13, 40, 20, 10, 5, 16, 8, 4, 2, 1	17	Yes
8	8, 4, 2, 1	4	No
9	9, 28, 14, 7, 22, 11, 34, 17, 52, 26, 13, 40, 20, 10, 5, 16, 8, 4, 2, 1	20	Yes
10	10, 5, 16, 8, 4, 2, 1	7	No

The method call Hailstone.propLong(10) returns 0.5, since 5 of the 10 hailstone sequences shown in the table are considered long.

A programmer wishes to complete the **propLong** method as described in the **Hailstone** class definition so that it most efficiently returns the proportion of long hailstone sequences with starting values between 1 and **n**, inclusive.

Write a description of how you would design the **propLong** method. You may assume that the methods **hailStoneLength** and **isLongSequence** work as specified and return data as shown in the table above.

Make sure to include the following in your response.

- Write the method header for the **propLong** method.
- Identify any existing method(s) in the Hailstone class that would be useful in designing and implementing the propLong method. Do not write the program code for this change.
- Describe how any existing method(s) in the **Hailstone** class would be implemented in **propLong** method.

(b)

Class information for this question

public class Hailstone

public static int hailstoneLength(int n)
public static boolean isLongSeq(int n)
public static double propLong(int n)

STOP

END OF THE MOCK EXAM